

BIO 4AE3. 17 Sep 2025

ESTIMATING R_0 (or R_t)



estimate the parameters

given the model, $R_0 = \frac{\beta}{\gamma} \cdot N$

rate of new infections (incidence) =

$$\beta \cdot S \cdot I$$

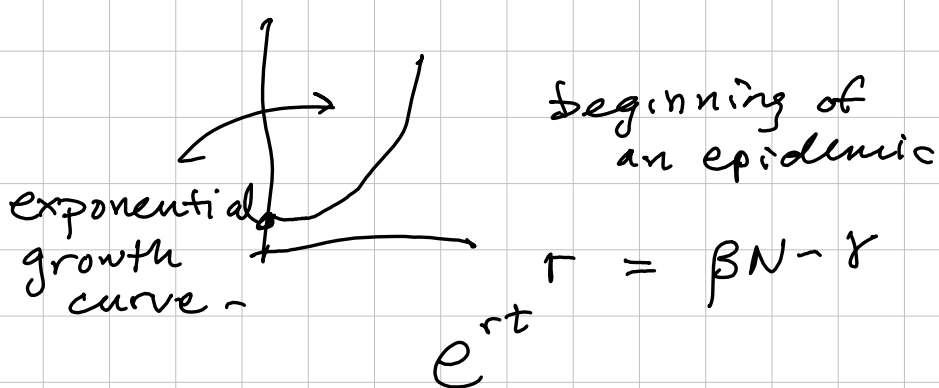
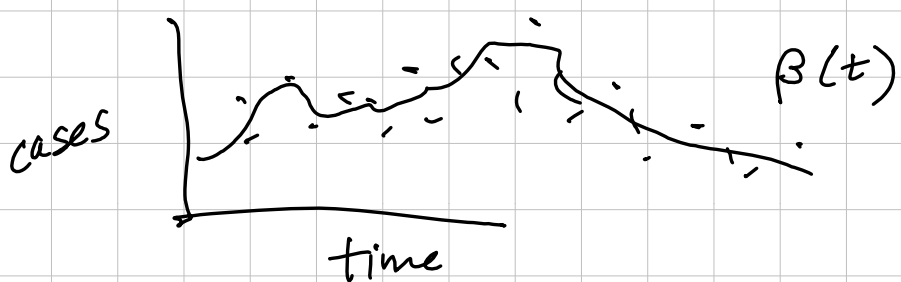
in a susceptible pop $\rightarrow \beta \cdot N \cdot I$

per infected person $\rightarrow \beta \cdot N$ (time⁻¹)

rate of recovery = γ

$\rightarrow$ infectious period = $1/\gamma$ (time)

$\rightarrow \frac{\beta N}{\gamma} \leftarrow$ individual-level



$$R_t^* = 1$$

$$R_t = R_0 \cdot \frac{S}{N}$$

$$I = R_0 \cdot \frac{S^*}{N}$$

$\rightarrow$ SEROSURVEYS.

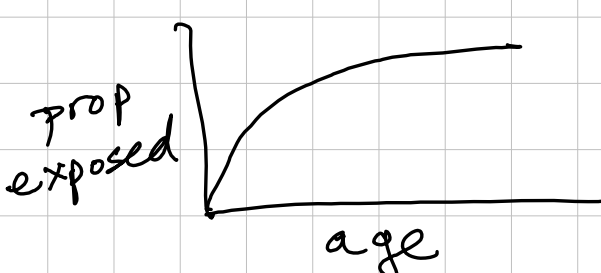
brucellosis
in bison.

Recovered/immune

$$I \approx 0$$

exposure surveys?

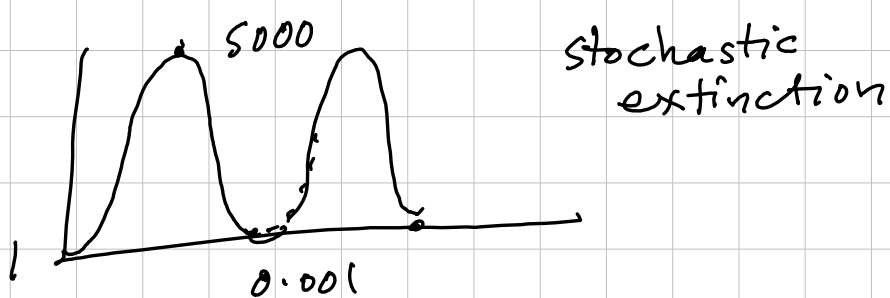
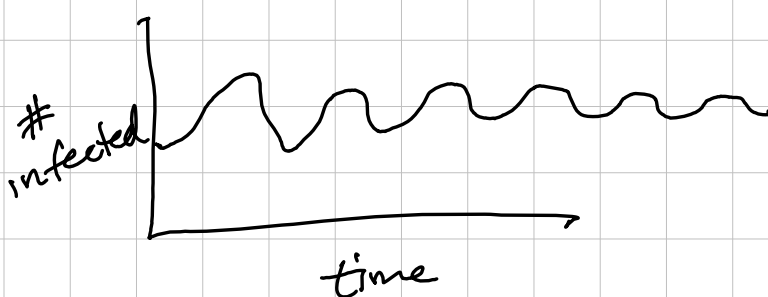
age-dependent exposure curves



DYNAMICS

SIR model predicts

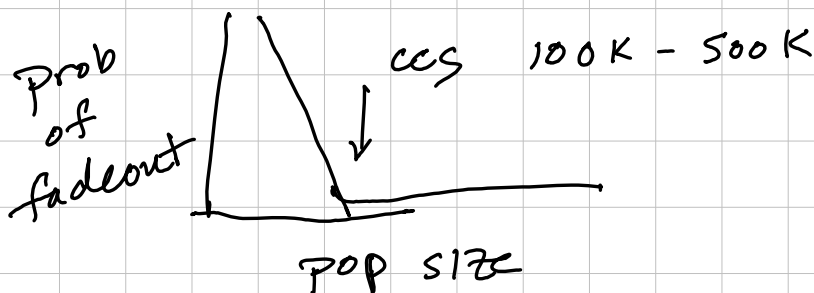
damped oscillations



dep on pop size, R_0 , host pop growth rate...

• CRITICAL community size.

$$R_0 \approx 18$$



• PERSISTENT cycles.

seasonal forcing

evolution / strain shift

Stochasticity