

intro

Ben Bolker

17 Oct 2018



Licensed under the Creative Commons [attribution-noncommercial license](#) Please share & remix noncommercially, mentioning its origin.

```
## Warning: S3 method
## 'ggplot2::autoplot.microbenchmark' was
## declared in NAMESPACE but not found
```

Logistics

- contact info, e-mail policies
- textbook
- assignments & grading
- policies: group work, take-home exams, etc.

Scope

- Topics
 - core:
 - * linear models: design matrices, contrasts, etc.
 - * core GLMs: binary (logistic/probit), binomial, Poisson regression
 - * weird GLMs and further topics: complete separation, overdispersion, Gamma models, non-standard links, use of offsets
 - * more weird GLMs: ordinal, negative binomial, zero-inflated
 - * GL mixed Ms: longitudinal / hierarchical / multilevel models
 - * Bayesian methods
 - “extraneous”
 - * data wrangling, visualization, and reproducible research: R, [ggplot](#), [tidyverse](#), [Rmarkdown](#)
 - * data visualization; graphical approaches to diagnostics and model interpretation
 - * best practices/ethics for data analysis
- Procedures
 - data exploration
 - model fitting (estimation)

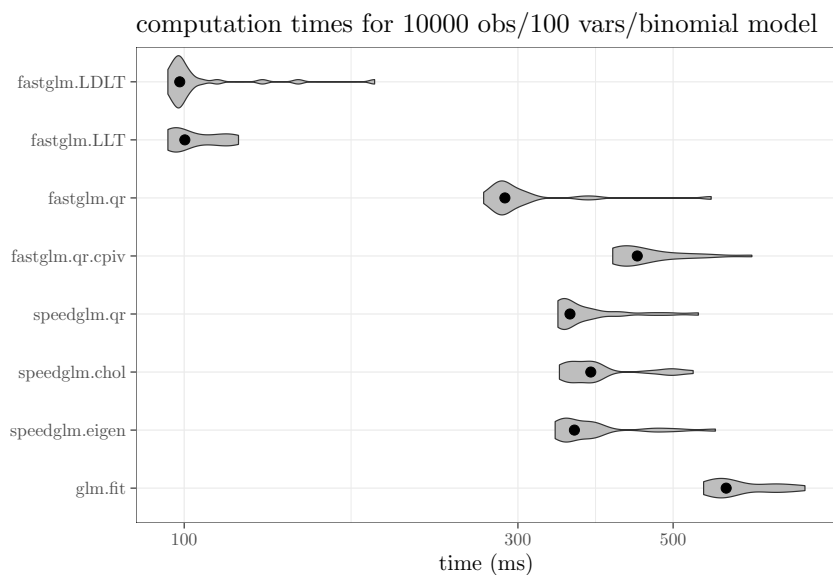
- graphical and numerical diagnostics
- inference
(Wald, likelihood, bootstrapping, AIC, ...)
- verbal and graphical presentation/interpretation of results

What is a GLM?

- handles any linear model
- *link function* specifies nonlinearity between linear predictor and response
- response distribution from the *exponential family*
(Gaussian, binomial, Poisson, Gamma, ...)

Why GLMs?

- robust
- fast
- sensible, flexible statistical models
- “sweet spot” in generality and power



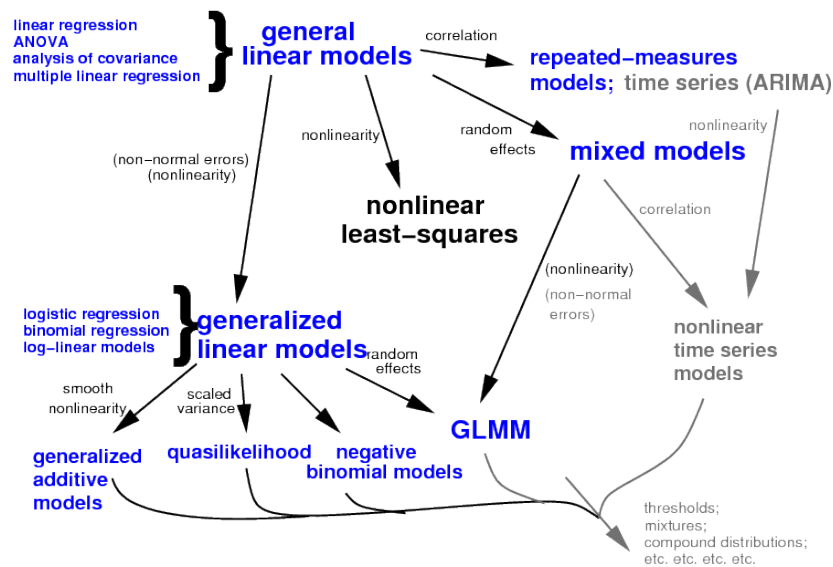
Example

Using data on AIDS diagnoses from Australia (Dobson and Barnett p. 69). Read in data and inspect it:

```

aids <- read.csv("../data/aids.csv")
head(aids)      ## beginning of data
summary(aids)  ## min/mean/max etc.
skimr::skim(aids) ## fancier

```



```
## construct useful date/index variables
aids <- transform(aids,
                  date=year+(quarter-1)/4,
                  index=seq(nrow(aids)))
```

Some basic pictures: base graphics

```
with(aids, plot(date, cases))
```



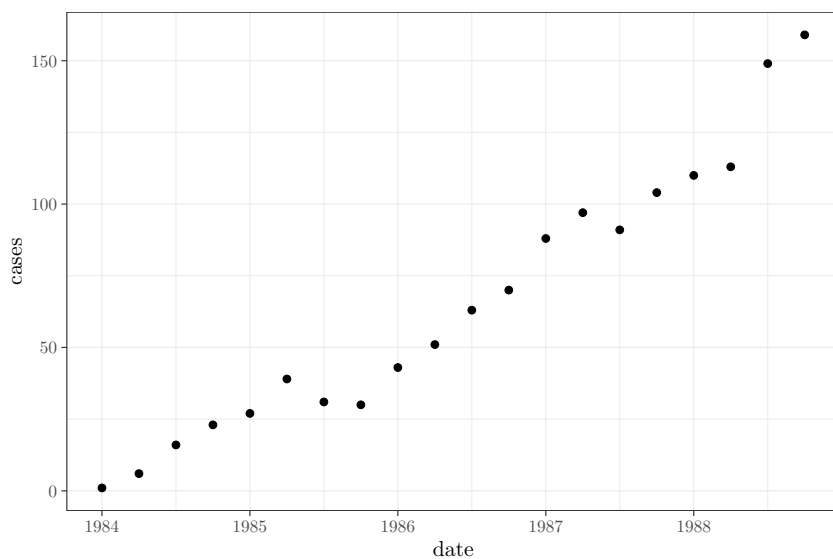
or with ggplot2

```
library(ggplot2)
theme_set(theme_bw()) ## get rid of grey background
## simple X/Y scatterplot
p0 <- (ggplot(aids, aes(x=date, y=cases))
```

```

+ geom_point() ## add points
)
print(p0)

```

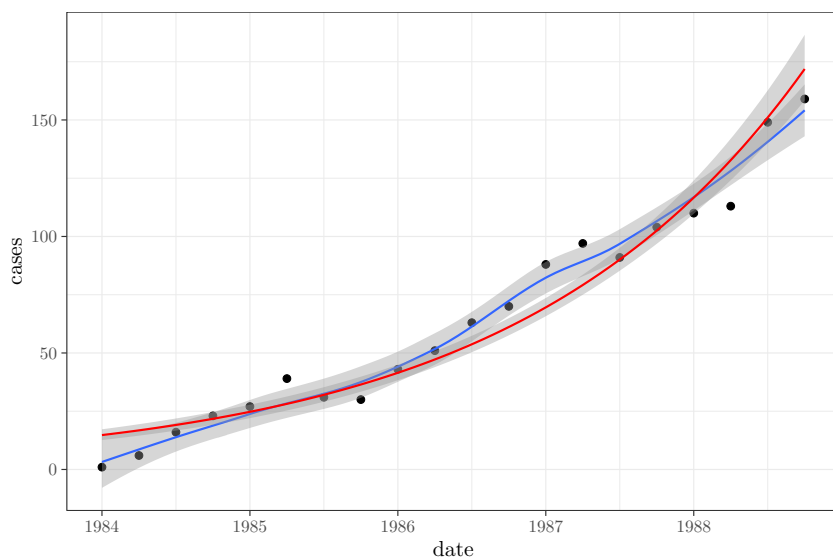


Now pictures with nonparametric and GLM fits superimposed:

```

(p0
+ geom_smooth() ## nonparametric
+ geom_smooth(method="glm",
              method.args=list(family=poisson),
              colour="red") ## GLM fit
)

```

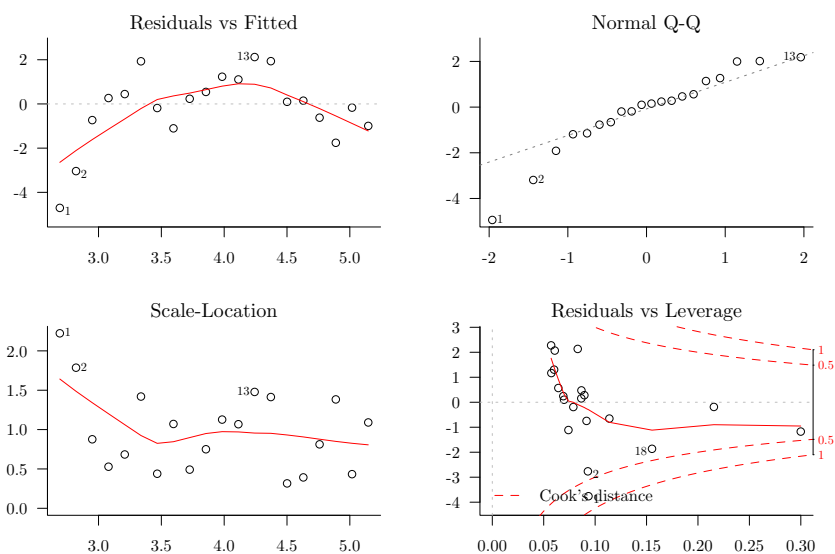


Fit a model using `glm()`:

```
g1 <- glm(cases~date, data=aids, family=poisson)
```

Diagnostic plots:

```
## set 2x2 grid of plots, tweak margins, label orientation
op <- par(mfrow=c(2,2),mar=c(3,3,2,2),
         las=1,bty="l")
plot(g1) ## plot standard diagnostics
```

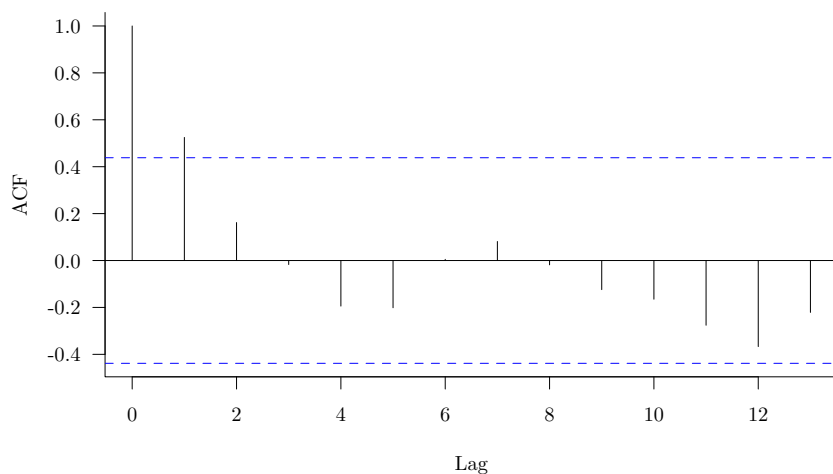


```
par(op) ## restore parameter settings
```

Check for temporal autocorrelation:

```
acf(residuals(g1))
```

Series residuals(g1)



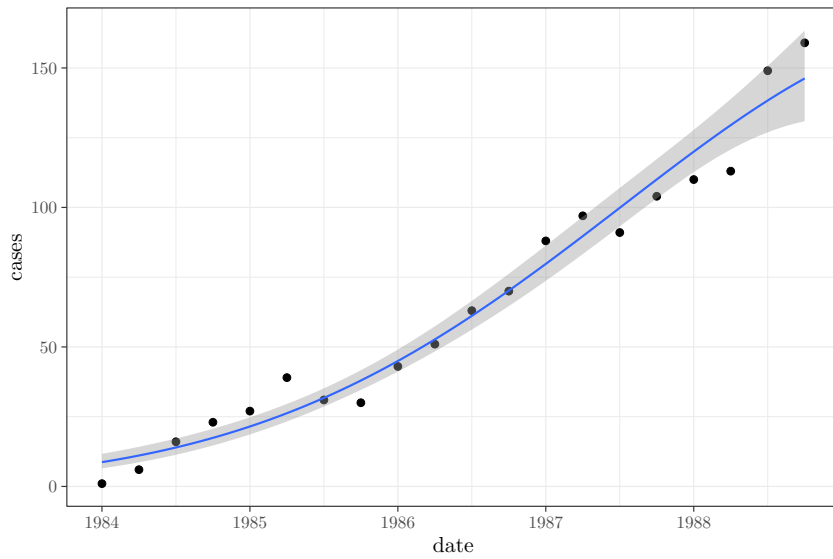
We have some problems. Will a quadratic fit help?

```
## poly(.,2) sets up a degree-2 (quadratic) polynomial
g2 <- glm(cases~poly(date,2),aids,family=poisson)
summary(g2) ## quadratic term significantly negative
```

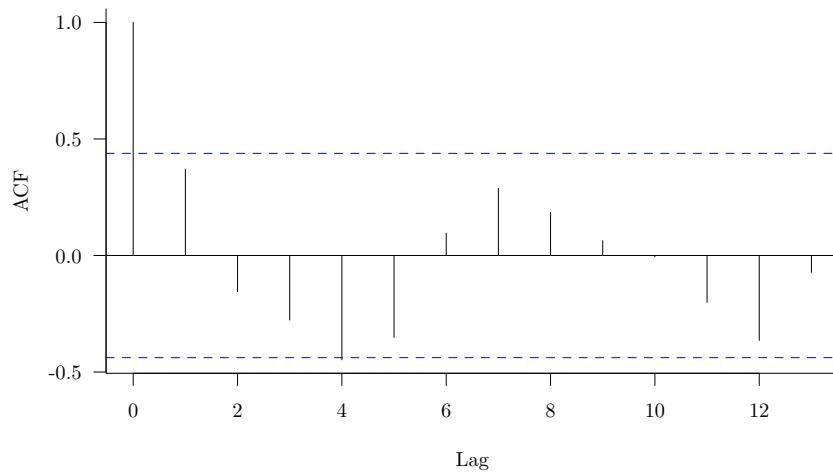
```
##
## Call:
## glm(formula = cases ~ poly(date, 2), family = poisson, data = aids)
##
## Deviance Residuals:
##      Min        1Q    Median        3Q        Max
## -3.3290  -0.9071  -0.0761   0.8985   2.3209
##
## Coefficients:
##              Estimate Std. Error z value
## (Intercept)   3.86859    0.03887  99.528
## poly(date, 2)1  3.82934    0.19545  19.592
## poly(date, 2)2 -0.68335    0.15315  -4.462
##              Pr(>|z|)
## (Intercept)   < 2e-16 ***
## poly(date, 2)1 < 2e-16 ***
## poly(date, 2)2 8.12e-06 ***
## ---
## Signif. codes:
##  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for poisson family taken to be 1)
##
##      Null deviance: 677.264  on 19  degrees of freedom
## Residual deviance:  31.992  on 17  degrees of freedom
## AIC: 150.29
##
## Number of Fisher Scoring iterations: 4
```

A picture of the same model fit:

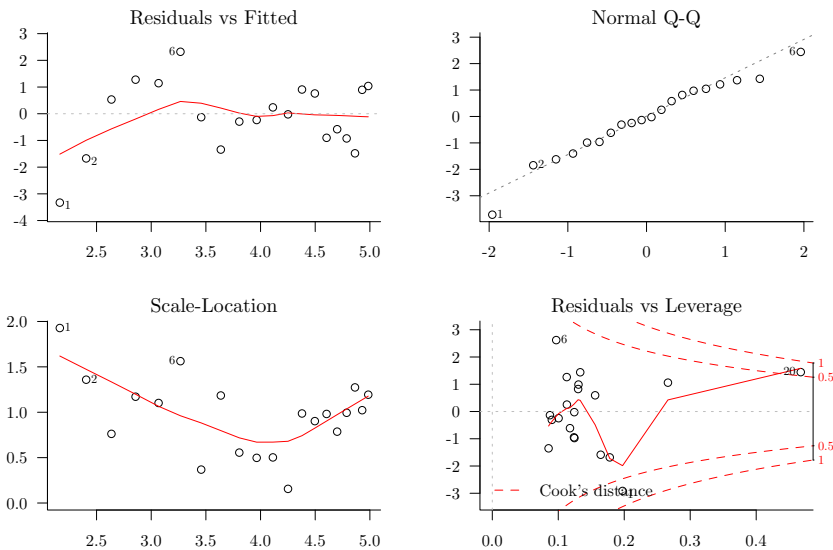
```
(p0
  +geom_smooth(method="glm",
               formula=y~poly(x,2),
               method.args=list(family=poisson))
)
```



Looks like the diagnostics and autocorrelation are better now ...
Series residuals(g2)



```
op <- par(mfrow=c(2,2),mar=c(3,3,2,2),
          las=1,bty="l") ## tweak params as before
plot(g2)
```



```
par(op) ## restore parameter settings
```

Power-law model

Despite stating that “[i]n the early phase of the epidemic, the numbers of cases seemed to be increasing exponentially”, Dobson and Barnett (2008) suggest fitting a power-law model of the form $Y \sim \text{Poisson}(\lambda = t^\theta)$ to the data instead:

```
g3 <- glm(cases~log(index), data=aids, family=poisson)
```

This fits pretty well, in fact much better than even the Gaussian (quadratic-exponential) model (not shown ...).

```
##           Estimate Std. Error z value
## (Intercept)  0.9960    0.1697   5.87
## log(index)   1.3266    0.0646  20.53
##           Pr(>|z|)
## (Intercept)  4.4e-09 ***
## log(index)   < 2e-16 ***
## ---
## Signif. codes:
##  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- The intercept is near 1; did we already know that 1984 was the origination year of AIDS in Australia (in which case $\text{AIDS}(1)=1$)?
- The power law model is $\text{AIDS}(t) \propto t^{1.33}$, with 95% confidence intervals on the exponent of $\{1.2, 1.46\}$ — what does that mean biologically/epidemiologically?

This turns out, like almost every problem, to be interesting and a bit challenging when you look at it carefully (see [Andrew Gelman](#) on “god is in every leaf of every tree” - but also consider Tukey “Far better an approximate answer to the *right* question, which is often vague, than an *exact* answer to the wrong question, which can always be made precise” or Grenfell “don’t overegg the pudding”

References

Dobson, Annette J., and Adrian Barnett. 2008. *An Introduction to Generalized Linear Models, Third Edition*. 3rd ed. Chapman; Hall/CRC.